

# CORE TRANSFORM DESIGN FOR HIGH EFFICIENCY VIDEO CODING (HEVC)

Jie Dong, Yan Ye

InterDigital Communications, LLC.

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# Core Transform in HEVC

- HEVC -- High Efficiency Video Coding
  - Emerging video coding standard developed by JCT-VC of ITU-T/VCEG and ISO/IEC/MPEG.
  - Focused on HD and ultra HD videos
  - Coding unit size up to  $2^K \times 2^K$  ( $K$  set in SPS)
  - Transform size scaled accordingly
    - $16 \times 16$  and  $32 \times 32$  for large homogeneous regions
    - $4 \times 4$  and  $8 \times 8$  for detail-rich regions
- Highly desired features in integer transform design
  - High energy compaction capability
  - Equal  $L^2$  norms of basis vectors
  - Orthogonal
  - Flexibility in implementation (matrix multiplication and fast algorithm)
  - 16-bit integer arithmetic

# Factorizable Transform Matrices

- Even-Odd Part Decomposition
  - Order- $2N$  DCT matrix  $\mathbf{T}_{DCT}^{(2N)}$

$$\mathbf{T}_{DCT}^{(2N)} = \begin{bmatrix} \frac{1}{\sqrt{2}} \mathbf{T}_{DCT}^{(N)} & 0 \\ 0 & \mathbf{P}_{DCT}^{(N)} \end{bmatrix} \begin{bmatrix} \mathbf{I}_N & \mathbf{J}_N \\ \mathbf{I}_N & -\mathbf{J}_N \end{bmatrix}$$

- Proposed order- $2N$  integer transform matrix  $\mathbf{T}_{2N}$

$$\mathbf{T}_{2N} = \begin{bmatrix} s_N \mathbf{T}_N & 0 \\ 0 & \mathbf{P}_N \end{bmatrix} \begin{bmatrix} \mathbf{I}_N & \mathbf{J}_N \\ \mathbf{I}_N & -\mathbf{J}_N \end{bmatrix}$$

$$\mathbf{T}_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

# Factorizable Transform Matrices (Order-8)

- Odd Part of Order-8 DCT  $\mathbf{P}_{DCT}^{(4)}$

$$\mathbf{P}_{DCT}^{(4)} = \begin{bmatrix} A_4 & B_4 & C_4 & D_4 \\ B_4 & -D_4 & -A_4 & -C_4 \\ C_4 & -A_4 & D_4 & B_4 \\ D_4 & -C_4 & B_4 & -A_4 \end{bmatrix} = \begin{bmatrix} \frac{1}{\sqrt{2}}(B_4 + C_4) & \frac{1}{\sqrt{2}}(A_4 + D_4) & \frac{1}{\sqrt{2}}(A_4 - D_4) & \frac{1}{\sqrt{2}}(B_4 - C_4) \\ & B_4 & -D_4 & -A_4 \\ & C_4 & -A_4 & D_4 \\ \frac{1}{\sqrt{2}}(B_4 - C_4) & -\frac{1}{\sqrt{2}}(A_4 - D_4) & \frac{1}{\sqrt{2}}(A_4 + D_4) & -\frac{1}{\sqrt{2}}(B_4 + C_4) \end{bmatrix}$$

- Elements' magnitudes

$$[A_4, B_4, C_4, D_4] = \left[ \frac{1}{2} \cos\left(\frac{\pi}{16}\right), \frac{1}{2} \cos\left(\frac{3\pi}{16}\right), \frac{1}{2} \cos\left(\frac{5\pi}{16}\right), \frac{1}{2} \cos\left(\frac{7\pi}{16}\right) \right]$$

[1] C. Loeffler, A. Ligtenberg, and G. S. Moschytz, "Practical fast 1-D DCT algorithms with 11 multiplications," in *Proc. IEEE Int. Conf. Acoust. Speech Signal Process.*, vol. 2. May 1989, pp. 988–991.

# Factorizable Transform Matrices (Order-8)

- Odd part of the Proposed Order-8 Integer Transform

$$\mathbf{P}_4 = \begin{bmatrix} h_4 e_4 (b_4 + c_4) & h_4 f_4 (a_4 + d_4) & h_4 f_4 (a_4 - d_4) & h_4 e_4 (b_4 - c_4) \\ k_4 j_4 b_4 & -k_4 i_4 d_4 & -k_4 i_4 a_4 & -k_4 j_4 c_4 \\ k_4 j_4 c_4 & -k_4 i_4 a_4 & k_4 i_4 d_4 & k_4 j_4 b_4 \\ h_4 e_4 (b_4 - c_4) & -h_4 f_4 (a_4 - d_4) & h_4 f_4 (a_4 + d_4) & -h_4 e_4 (b_4 + c_4) \end{bmatrix}$$

$$= \begin{bmatrix} h_4 & 0 & 0 & h_4 \\ 0 & 0 & k_4 & 0 \\ 0 & k_4 & 0 & 0 \\ h_4 & 0 & 0 & -h_4 \end{bmatrix} \times \begin{bmatrix} e_4 & 0 & f_4 & 0 \\ 0 & -i_4 & 0 & j_4 \\ j_4 & 0 & -i_4 & 0 \\ 0 & f_4 & 0 & e_4 \end{bmatrix} \times \begin{bmatrix} a_4 & 0 & 0 & -b_4 \\ 0 & c_4 & -d_4 & 0 \\ 0 & d_4 & c_4 & 0 \\ b_4 & 0 & 0 & a_4 \end{bmatrix}$$

- Elements' Relation 1

1.  $(b_4 + c_4)/(b_4 - c_4) \approx a_4/d_4 \approx A_4/D_4$  and  $(a_4 + d_4)/(a_4 - d_4) \approx b_4/c_4 \approx B_4/C_4$
2.  $(i_4 a_4)/(j_4 b_4) \approx (e_4 (b_4 + c_4))/(f_4 (a_4 + d_4)) \approx A_4/B_4$
3.  $h_4 f_4 (a_4 + d_4) \approx k_4 j_4 b_4$  and  $h_4 e_4 (b_4 + c_4) \approx k_4 i_4 a_4$

# Factorizable Transform Matrices (Order-16)

- Odd Part of Order-16 DCT  $\mathbf{P}_{DCT}^{(8)}$

$$\mathbf{P}_{DCT}^{(8)} = \begin{bmatrix} A_8 & B_8 & C_8 & D_8 & E_8 & F_8 & G_8 & H_8 \\ B_8 & E_8 & H_8 & -F_8 & -C_8 & -A_8 & -D_8 & -G_8 \\ C_8 & H_8 & -D_8 & -B_8 & -G_8 & E_8 & A_8 & F_8 \\ D_8 & -F_8 & -B_8 & H_8 & A_8 & G_8 & -C_8 & -E_8 \\ E_8 & -C_8 & -G_8 & A_8 & -H_8 & -B_8 & F_8 & D_8 \\ F_8 & -A_8 & E_8 & G_8 & -B_8 & D_8 & H_8 & -C_8 \\ G_8 & -D_8 & A_8 & -C_8 & F_8 & H_8 & -E_8 & B_8 \\ H_8 & -G_8 & F_8 & -E_8 & D_8 & -C_8 & B_8 & -A_8 \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{\sqrt{2}}(D_8 + E_8) & \frac{1}{\sqrt{2}}(C_8 + F_8) & \frac{1}{\sqrt{2}}(B_8 + G_8) & \frac{1}{\sqrt{2}}(A_8 + H_8) & \frac{1}{\sqrt{2}}(A_8 - H_8) & \frac{1}{\sqrt{2}}(B_8 - G_8) & \frac{1}{\sqrt{2}}(C_8 - F_8) & \frac{1}{\sqrt{2}}(D_8 - E_8) \\ E_8 I_8 + D_8 J_8 & -F_8 I_8 + C_8 J_8 & B_8 I_8 - G_8 J_8 & -A_8 I_8 - H_8 J_8 & H_8 I_8 - A_8 J_8 & -G_8 I_8 - B_8 J_8 & -C_8 I_8 - F_8 J_8 & D_8 I_8 - E_8 J_8 \\ D_8 I_8 + E_8 J_8 & -C_8 I_8 + F_8 J_8 & G_8 I_8 - B_8 J_8 & -H_8 I_8 - A_8 J_8 & -A_8 I_8 + H_8 J_8 & B_8 I_8 + G_8 J_8 & F_8 I_8 + C_8 J_8 & -E_8 I_8 + D_8 J_8 \\ D_8 & -F_8 & -B_8 & H_8 & A_8 & G_8 & -C_8 & -E_8 \\ E_8 & -C_8 & -G_8 & A_8 & -H_8 & -B_8 & F_8 & D_8 \\ -E_8 I_8 + D_8 J_8 & -F_8 I_8 - C_8 J_8 & B_8 I_8 + G_8 J_8 & A_8 I_8 - H_8 J_8 & -H_8 I_8 - A_8 J_8 & -G_8 I_8 + B_8 J_8 & -C_8 I_8 + F_8 J_8 & -D_8 I_8 - E_8 J_8 \\ -D_8 I_8 + E_8 J_8 & -C_8 I_8 - F_8 J_8 & G_8 I_8 + B_8 J_8 & H_8 I_8 - A_8 J_8 & A_8 I_8 + H_8 J_8 & B_8 I_8 - G_8 J_8 & F_8 I_8 - C_8 J_8 & E_8 I_8 + D_8 J_8 \\ \frac{1}{\sqrt{2}}(D_8 - E_8) & -\frac{1}{\sqrt{2}}(C_8 - F_8) & \frac{1}{\sqrt{2}}(B_8 - G_8) & -\frac{1}{\sqrt{2}}(A_8 - H_8) & \frac{1}{\sqrt{2}}(A_8 + H_8) & -\frac{1}{\sqrt{2}}(B_8 + G_8) & \frac{1}{\sqrt{2}}(C_8 + F_8) & -\frac{1}{\sqrt{2}}(D_8 + E_8) \end{bmatrix}$$

$$[A_8, B_8, C_8, \dots, G_8, H_8] = \left[ \frac{1}{\sqrt{8}} \cos\left(\frac{\pi}{32}\right), \frac{1}{\sqrt{8}} \cos\left(\frac{3\pi}{32}\right), \frac{1}{\sqrt{8}} \cos\left(\frac{5\pi}{32}\right), \frac{1}{\sqrt{8}} \cos\left(\frac{7\pi}{32}\right), \dots, \frac{1}{\sqrt{8}} \cos\left(\frac{13\pi}{32}\right), \frac{1}{\sqrt{8}} \cos\left(\frac{15\pi}{32}\right) \right]$$

# Factorizable Transform Matrices (Order-16)

- Odd part of the Proposed Order-16 Integer Transform

$$P_8 = \begin{bmatrix} l_8(d_8 + e_8) & l_8(c_8 + f_8) & l_8(b_8 + g_8) & l_8(a_8 + h_8) & l_8(a_8 - h_8) & l_8(b_8 - g_8) & l_8(c_8 - f_8) & l_8(d_8 - e_8) \\ e_8i_8 + d_8j_8 & -f_8i_8 + c_8j_8 & b_8i_8 - g_8j_8 & -a_8i_8 - h_8j_8 & h_8i_8 - a_8j_8 & -g_8i_8 - b_8j_8 & -c_8i_8 - f_8j_8 & d_8i_8 - e_8j_8 \\ d_8i_8 + e_8j_8 & -c_8i_8 + f_8j_8 & g_8i_8 - b_8j_8 & -h_8i_8 - a_8j_8 & -a_8i_8 + h_8j_8 & b_8i_8 + g_8j_8 & f_8i_8 + c_8j_8 & -e_8i_8 + d_8j_8 \\ k_8d_8 & -k_8f_8 & -k_8b_8 & k_8h_8 & k_8a_8 & k_8g_8 & -k_8c_8 & -k_8e_8 \\ k_8e_8 & -k_8c_8 & -k_8g_8 & k_8a_8 & -k_8h_8 & -k_8b_8 & k_8f_8 & k_8d_8 \\ -e_8i_8 + d_8j_8 & -f_8i_8 - c_8j_8 & b_8i_8 + g_8j_8 & a_8i_8 - h_8j_8 & -h_8i_8 - a_8j_8 & -g_8i_8 + b_8j_8 & -c_8i_8 + f_8j_8 & -d_8i_8 - e_8j_8 \\ -d_8i_8 + e_8j_8 & -c_8i_8 - f_8j_8 & g_8i_8 + b_8j_8 & h_8i_8 - a_8j_8 & a_8i_8 + h_8j_8 & b_8i_8 - g_8j_8 & f_8i_8 - c_8j_8 & e_8i_8 + d_8j_8 \\ l_8(d_8 - e_8) & -l_8(c_8 - f_8) & l_8(b_8 - g_8) & -l_8(a_8 - h_8) & l_8(a_8 + h_8) & -l_8(b_8 + g_8) & l_8(c_8 + f_8) & -l_8(d_8 + e_8) \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 & l_8 & -l_8 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -j_8 & i_8 \\ i_8 & j_8 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & k_8 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & k_8 & 0 & 0 \\ j_8 & -i_8 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & i_8 & j_8 \\ 0 & 0 & 0 & l_8 & l_8 & 0 & 0 & 0 \end{bmatrix} \times \begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & -1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} -1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & -1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & -1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} d_8 & 0 & 0 & 0 & 0 & 0 & 0 & -e_8 \\ 0 & f_8 & 0 & 0 & 0 & 0 & c_8 & 0 \\ 0 & 0 & b_8 & 0 & 0 & -g_8 & 0 & 0 \\ 0 & 0 & 0 & h_8 & a_8 & 0 & 0 & 0 \\ 0 & 0 & 0 & -a_8 & h_8 & 0 & 0 & 0 \\ 0 & 0 & g_8 & 0 & 0 & b_8 & 0 & 0 \\ 0 & -c_8 & 0 & 0 & 0 & 0 & f_8 & 0 \\ e_8 & 0 & 0 & 0 & 0 & 0 & 0 & d_8 \end{bmatrix}$$

- Elements' Relation 2

- $a_8 : b_8 : c_8 : d_8 : e_8 : f_8 : g_8 : h_8 \approx A_8 : B_8 : C_8 : D_8 : E_8 : F_8 : G_8 : H_8$

- $i_8 : j_8 : k_8 : l_8 \approx \cos\left(\frac{3\pi}{8}\right) : \sin\left(-\frac{3\pi}{8}\right) : 1 : \frac{1}{\sqrt{2}}$

# Factorizable Transform Matrices (Order-32)

- Odd Part of Order-32 DCT  $\mathbf{P}_{DCT}^{(16)}$ 
  - Factorization proposed by Chen *et al.* cause high latency

$$\mathbf{P}_{DCT}^{(16)} = \mathbf{R}_7 \times \mathbf{R}_6 \times \mathbf{R}_5 \times \mathbf{R}_4 \times \mathbf{R}_3 \times \mathbf{R}_2 \times \mathbf{R}_1$$

- Odd Part of the Proposed Order-32 Integer Transform

$$\mathbf{P}_{16} = \mathbf{W} \times \mathbf{M}_4 \times \mathbf{M}_3 \times \mathbf{M}_2 \times \mathbf{M}_1$$

- $\mathbf{M}_3, \mathbf{M}_1$  approximate  $\mathbf{R}_3, \mathbf{R}_1$
- $\mathbf{R}_4, \mathbf{R}_2$  are binary matrices and the same as  $\mathbf{M}_4, \mathbf{M}_2$
- $\mathbf{W}$  approximate  $\mathbf{R}_7 \times \mathbf{R}_6 \times \mathbf{R}_5$

[2] W. H. Chen, C. H. Smith, and S. C. Fralick, "A fast computational algorithm for the discrete cosine transform", *IEEE Trans. Commun.*, vol. 25, no. 9, pp.1004-1009, Sept. 1977.



# Factorizable Transform Matrices (Order-32)

$$\mathbf{M}_1 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 & 0 & 0 & -x_1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 & -x_1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & -x_1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_1 & -x_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_1 & x_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & x_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & x_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & x_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & x_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ x_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\mathbf{M}_3 = \begin{bmatrix} y_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & y_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -y_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_1 & 0 \\ 0 & 0 & 0 & -y_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_1 & 0 \\ 0 & 0 & 0 & 0 & -y_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -y_2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -y_1 & 0 & 0 & 0 & 0 & -y_2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & y_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -y_2 & 0 & 0 & 0 & y_1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -y_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_1 & 0 \\ 0 & 0 & 0 & 0 & y_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & y_0 \end{bmatrix}$$

- Elements' Relation 3

1.  $x_0 : x_1 \approx \sqrt{2} : 1$

2.  $y_0 : y_1 : y_2 \approx 1 : \sin\left(\frac{\pi}{8}\right) : \cos\left(\frac{\pi}{8}\right)$

# Factorizable Transform Matrices (Order-32)

- Odd Part of the Proposed Order-32 Integer Transform

$$\mathbf{P}_{16} = \mathbf{W} \times \mathbf{M}_4 \times \mathbf{M}_3 \times \mathbf{M}_2 \times \mathbf{M}_1$$

$$\mathbf{W} = \mathbf{Z} \times \mathbf{X} \times \mathbf{Y}$$

- $\mathbf{Z}, \mathbf{Y}$  are binary matrices with only one non-zero element in each row/column, used for re-ordering.
- $\mathbf{X}$  is the only effective matrix in  $\mathbf{W}$ .

$$\mathbf{X} = \begin{bmatrix} \mathbf{X}_1 & 0 & 0 & 0 \\ 0 & \mathbf{X}_2 & 0 & 0 \\ 0 & 0 & \mathbf{X}_3 & 0 \\ 0 & 0 & 0 & \mathbf{X}_4 \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{X}_1 = & p_0 & p_1 & p_2 & p_3 \\ p_4 & p_5 & -p_6 & p_7 \\ -p_7 & -p_6 & -p_5 & p_4 \\ -p_3 & p_2 & -p_1 & p_0 \end{bmatrix} \begin{bmatrix} \mathbf{X}_2 = & q_0 & q_1 & q_2 & q_3 \\ -q_4 & q_5 & q_6 & -q_7 \\ -q_7 & -q_6 & q_5 & q_4 \\ q_3 & -q_2 & q_1 & -q_0 \end{bmatrix} \begin{bmatrix} \mathbf{X}_3 = & r_0 & r_1 & r_2 & r_3 \\ r_4 & r_5 & -r_6 & r_7 \\ -r_7 & -r_6 & -r_5 & r_4 \\ -r_3 & r_2 & -r_1 & r_0 \end{bmatrix} \begin{bmatrix} \mathbf{X}_4 = & v_0 & v_1 & v_2 & -v_3 \\ -v_4 & v_5 & v_6 & -v_7 \\ -v_7 & -v_6 & v_5 & v_4 \\ -v_3 & -v_2 & v_1 & -v_0 \end{bmatrix}$$

# Core Transform Design Proposed for HEVC

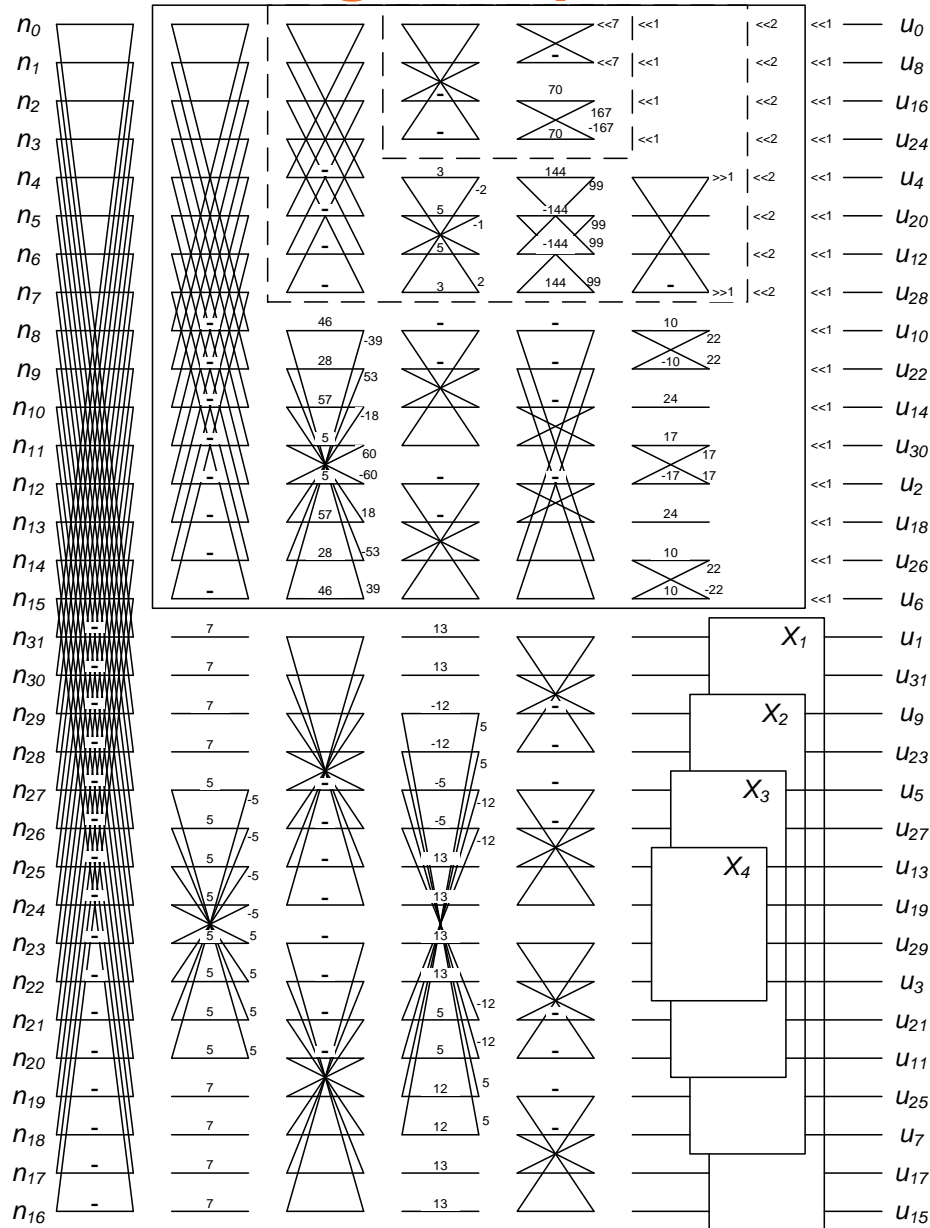
- Use the proposed general transform matrices
- Brute-force search for the matrix elements based on
  - Element relations
  - Almost equal  $L^2$  norms of the basis vectors
  - Negligible deviation from DCT [3]
  - Negligible transform error introduced by non-orthogonality [4]

<b>Order-4</b>	$a_2, b_2$	167	70						
<b>Order-8</b>	$a_4, b_4, c_4, d_4, e_4, f_4, i_4, j_4, h_4, k_4$	3	2	5	1	144	99	72	99
<b>Order-16</b>	$a_8, b_8, c_8, d_8, e_8, f_8, g_8, h_8$	60	57	53	46	39	28	18	5
	$i_8, j_8, k_8, l_8$	10	-22	24	17				
<b>Order-32</b>	$x_0, x_1$	7	5						
	$y_0, y_1, y_2$	13	5	12					
	$p_0, p_1, p_2, p_3, p_4, p_5, p_6, p_7$	1	5	31	32	23	19	26	21
	$q_0, q_1, q_2, q_3, q_4, q_5, q_6, q_7$	31	13	28	8	16	30	11	27
	$r_0, r_1, r_2, r_3, r_4, r_5, r_6, r_7$	8	21	23	31	27	2	32	16
	$v_0, v_1, v_2, v_3, v_4, v_5, v_6, v_7$	30	19	25	10	29	31	5	13
<b><math>S_N</math></b>	$s_2, s_4, s_8, s_{16}$	128	2	4	2				

[3] M. Wien and S. Sun, "ICT comparison for adaptive block transforms," document VCEG-L12, ITU-T SG16/Q6, Jan. 2001.

[4] J. Dong, K. N. Ngan, C. K. Fong, and W. K. Cham, "2D order-16 integer transforms for HD video coding," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 19, no. 10, pp. 1463–1474, Oct. 2009.

# Core Transform Design Proposed for HEVC



# Experimental Results

- Integrated into HM4.0 using 16-bit integer arithmetic
- Tested under common test condition for and special test condition of CE10
- Compared with other core transform designs in CE10
- Rate-Distortion Performance: less than 1% BD-rate difference under various test settings and QPs

[5] A. Fuldseth, G. Bjøntegaard, and M. Budagavi, "CE10: core transform design for HEVC," document JCTVC-G495, Joint Collaborative Team on Video Coding, Nov. 2011.

[6] R. Joshi, J. Sole, and M. Karczewicz, "CE10: Scaled integer transforms supporting recursive factorization structure," document JCTVC-G579, Joint Collaborative Team on Video Coding, Nov. 2011.

[7] E. Alshina *et al.*, "CE10: full factorization core transforms for HEVC," document JCTVC-G737, Joint Collaborative Team on Video Coding, Nov. 2011.

# Experimental Results

- Features offered by each core transform design

	Small DCT distortion	Full factorization	No scaling process	Negligible transform error	Flexible implementation
Cisco's	√		√	√	√
Qualcomm's	√	√		√	
Samsung's	√	√	√	√	√
Proposed	√	√	√	√	√

- Numbers of arithmetic operations for  $N$ -point 1-D transform

		Cisco's	Qualcomm's	Samsung's	Proposed
4-point	+	8	9	9	9
	×	6	3	3	3
8-point	+	28	26	29	31
	×	22	12	11	11
16-point	+	100	72	81	93
	×	86	36	31	21
32-point	+	372	186	229	279
	×	342	92	87	56

# Conclusion

- Propose the core transform design for HEVC
  - Factorizable general transform matrices
  - Matrix elements
- Features offered
  - High energy compaction capability
  - No scaling process
  - Negligible transform error introduced by non-orthogonality
  - Flexible implementations
  - 16-bit integer arithmetic
- R-D performance
  - Less than 1% BD-rate difference under various test settings